
1 (5 pts). Write as a single logarithm: $4 \ln(x - 1) - \frac{1}{3} \ln(3x + 6) + 2 \ln(3x + 2)$

2 (5 pts). Write entirely in terms of logs of linear functions: $\log_2 \left(\frac{x^2 - x - 2}{4x^2 + 3x - 1} \right)$

Solution:

1.(Source: 5.2.more.3f) Using the properties of logarithms (Theorem 5.2.1, p. 340),

$$\begin{aligned} 4 \ln(x - 1) - \frac{1}{3} \ln(3x + 6) + 2 \ln(3x + 2) &= \ln(x - 1)^4 + \ln(3x + 6)^{-1/3} + \ln(3x + 2)^2 \\ &= \ln \left((x - 1)^4 (3x + 6)^{-1/3} (3x + 2)^2 \right), \end{aligned}$$

which, according to the directions, is all that's required. If you like, this could be written as

$$\ln \left(\frac{(x - 1)^4 (3x + 2)^2}{(3x + 6)^{1/3}} \right),$$

or even

$$\ln \left(\frac{(x - 1)^4 (3x + 2)^2}{\sqrt[3]{3x + 6}} \right)$$

2.(Source: 5.2.more.2i) Factor the quadratics:

$$\log_2 \left(\frac{x^2 - x - 2}{4x^2 + 3x - 1} \right) = \log_2 \left(\frac{(x - 2)(x + 1)}{(4x - 1)(x + 1)} \right)$$

Cancel the common factor, and then break up using the properties of logs:

$$\log_2 \left(\frac{x - 2}{4x - 1} \right) = \log_2(x - 2) - \log_2(4x - 1)$$

(done)