

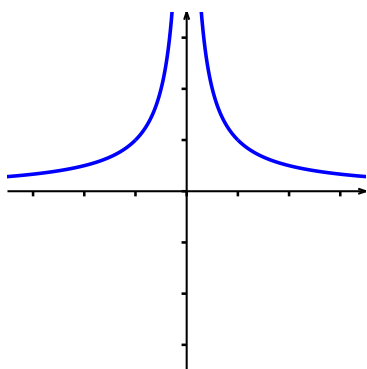
1 (10 pts). Sketch the graphs of the following functions. Include all asymptotes and their equations. Find all intercepts. Label your answers so I can tell your x -intercepts from your y -intercepts.

a. $f(x) = x^{-2/5}$

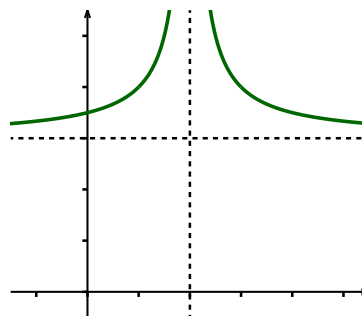
b. $g(x) = 3 + (x - 2)^{-2/5}$.

(Source: 2.2.more.1f)

1a. In the first quadrant, the graph of $y = x^{-2/5} = \frac{1}{(\sqrt[5]{x})^2}$ looks roughly like $y = x^{-1}$. The axes $y = 0$ and $x = 0$ are asymptotes because $|y|$ is huge when $|x|$ is tiny and tiny when $|x|$ is huge. $\sqrt[5]{x}$ is defined for negative x -values, and when we compute its square and take reciprocals, the result is positive, so the graph of $y = x^{-2/5}$ looks the graph on the left:



a. $y = x^{-2/5}$



b. $y = 3 + (x - 2)^{-2/5}$

1b. To obtain the graph of $y = 3 + (x - 2)^{-2/5}$, shift the graph up 3 and to the right 2. This makes the two new asymptotes $y = 3$ and $x = 2$. See the graph on the right.

As our drawing suggests, the graph has no x -intercept. This because when we set $y = 0$ and solve for x , we come to the equation

$$-3 = (x - 2)^{-2/5} = \left(\frac{1}{\sqrt[5]{x - 2}} \right)^2.$$

Since the right side is a square, this has no real solutions.

At $x = 0$, we calculate the y -intercept to be $y = 3 + (0 - 2)^{-2/5}$. Since $(-1)^{-2/5} = 1$, the y -intercept can be more simply written as either $3 + 2^{-2/5}$ or $3 + \frac{1}{\sqrt[5]{4}}$.